

Editorial

Minimizing the Cost in Sample Size Computation

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Editorial

While our society is hungry for new medical treatments that can bring hopes to millions of patients at the terminal of their lives, the medical experiment expenses are sky rocketing, funding sources for research are limited and shrinking. It is even worse that our research budgets for awarded proposals are often cut to a fraction of original planned spending. Therefore, it is very important for us to find methods for minimizing costs in medical studies. In 1977, Cochran [1] studied how to minimize the cost for survey samplings in his classic book. Ideal solution in sample size allocation is to maximize the power and minimize the cost with required significant level. Guo et al. [2] have some nice results in this area. Allison et al. [3] have discussed strategies in minimizing the financial cost while minimizing the cost, but their paper lacks depth in computing. Guo and Luh [4] have studied how to compute sample size with fixed cost for comparing two trimmed means. Luo, Wang and Meza [5] have proven the formulas of sample size with maximal precision for difference and ratio of two binary data and maximal power for detecting the difference of two proportions, two survival rates and two correlations under financial constraints. The free software for their results is available upon request. There are a lot of publications about cost-effectiveness-design (see [6,7] and accompanying references), but our approaches are totally different from them since we focus on sample size allocation at the design stage. Our methods are statistics with computational support.

As we conduct sample size computation for clinical trials with cost in mind, there are many questions for us to work on and much room for improvement. Since clinical trials are experiments on humans, we will face unpredictable things and corresponding costs are in some sense unpredictable. But there are still some rules that we can follow and a lot of things are within the control of our ability. That is why we have budget sheet in our research proposal. There are items for the cost of clinical trials that may be listed, say nurses, technicians, physicians, managers, medicines, compensation, insurance, tests, lab, etc., but we can classify them as two parts, one that is fixed cost, and the other will be proportional to the sample sizes of control and intervention groups. Let us assume the sample sizes for intervention and control are N_1 and N_2 , respectively, in a clinical trial and corresponding costs for each patient are C_1 and C_2 , respectively, then our interest is to minimize the costs from the second part at the design stage. The objective functions for minimization are the cost

functions related to sample sizes N_1 and N_2 , prices C_1 and C_2 , power, significant level, variances, and minimal detectable effect size. For example, if our interest is non-inferiority or superiority test for two proportions with the following hypotheses

$$H_0 : \pi_1 - \pi_2 \leq \Delta \text{ vs } H_1 : \pi_1 - \pi_2 > \Delta$$

Where π_1 and π_2 are the response rates in intervention and control, then the optimal sample allocation that minimizing the total cost is [8]

$$N_1 = \frac{[\pi_1(1-\pi_1)]^{\frac{1}{2}} \left([C_1\pi_1(1-\pi_1)]^{\frac{1}{2}} + [C_2\pi_2(1-\pi_2)]^{\frac{1}{2}} \right)}{C_1^{\frac{1}{2}} \left(\frac{\pi_1 - \pi_2}{z_\alpha + z_\beta} \right)^2}$$

$$N_2 = \frac{[\pi_2(1-\pi_2)]^{\frac{1}{2}} \left([C_1\pi_1(1-\pi_1)]^{\frac{1}{2}} + [C_2\pi_2(1-\pi_2)]^{\frac{1}{2}} \right)}{C_2^{\frac{1}{2}} \left(\frac{\pi_1 - \pi_2}{z_\alpha + z_\beta} \right)^2}$$

Note we do not have equal sample size allocation. Here equal sample size allocation does not save the budget. Luo et al. [8-10] have obtained a series of results in this area with required power and significant level under different conditions. Please see our follow-up papers for details. Another area that is to follow is what Luo, Wang, and Meza [5] have done and to work out results under financial constraints. Assume our given total cost under the above hypothesis is C and we want to test the difference of two independent sample means with normal distributions, then for the following hypotheses

$$H_0: \mu_1 = \mu_2 \text{ vs } H_1: \mu_1 \neq \mu_2$$

the following sample size allocation reaches maximal power [5]

$$N_1 = \frac{C\sigma_1}{\sqrt{C_1}(\sigma_1\sqrt{C_1} + \sigma_2\sqrt{C_2})}, \quad N_2 = \frac{C\sigma_2}{\sqrt{C_2}(\sigma_1\sqrt{C_1} + \sigma_2\sqrt{C_2})}$$

We deeply believe the results are useful and will be more efficient economically in the design of medical studies.

We also develop software available for all users for free. This is very important for the wide application of a statistical method that will be beneficial to all clinical trials. Our software will be published and available to public users. Software does not only test our methods, but also provides feedbacks for further development.

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